1 Introduction

The dynamical behaviour of glass-forming systems has long been the subject of intense research.1 One important feature of disordered systems is that the dynamics of density fluctuations is characterized by a two-step decay, which implies the presence of two main relaxation processes: a microscopic or fast relaxation, associated with the interactions between a particle and the cage of its nearest neighbors followed by a structural or slow relaxation process, related to the structural rearrangements of the particles. These two distinct processes have been observed in simple monatomic liquids,2 hydrogen bonded liquids,3,4 structural glasses,5–8 colloids9–11 and DNA nanostars.12 Furthermore Mode Coupling Theory (MCT)13 has predicted the evolution of the two relaxations when a system goes from the liquid to the arrested state: this may happen e.g. by changing the temperature, packing fraction or waiting time (aging). However, even if the supercooled liquid phase above the glass transition undergoes a transition from a diffusive to an activated regime, indicating an unchanged, diffusive single particle dynamics at short times, the structural relaxation shows a clear change in particle dynamics should occur, as found in numerical simulations,20,21 from diffusive to activated in the glass. The signature of this change at different length scales can be revealed by investigating the dependence of structural relaxation time changes from diffusive, characterized by a dependence, to a dependence in the full aging regime which marks a discontinuous hopping dynamics. Both regimes are associated with a stretched behaviour of the correlation functions. We expect these findings to provide a general description of both relaxations across the glass transition.

This is the aim of the present work where the aging investigation of a colloidal system makes possible a detailed study across the glass transition. In particular the waiting time and wavenumber dependence of both fast and slow relaxation times is monitored through a combination of multangle Dynamic Light Scattering (DLS), Neutron Spin Echo (NSE), X-ray Photon Correlation Spectroscopy (XPCS) and Molecular Dynamics (MD) simulations. In this way we access an unprecedentedly wide range of time and length scales and we find a different behaviour for the two relaxations across the glass transition. While the microscopic one remains unperturbed, indicating an unchanged, diffusive single particle dynamics at short times, the structural relaxation shows a clear change. Indeed, going from the liquid to the arrested state undergoes a transition from a dependence to a dependence. Previous studies in aqueous Laponite dispersions11,26 reported a dependence for both microscopic and structural relaxation.
times in the ergodic DLS regime. Later on studies on different systems e.g. colloids,27–28 clays,29–32 metallic glasses,33 polymers,34–36 and supercooled liquids37 reported a $Q^{-1}$ dependence of the structural relaxation time associated with an anomalous compressed exponential relaxation of the correlation functions attributed to hyperdiffusive dynamics.38 Differently, in the present study the relaxation curves at long times are always described by a stretched exponential, which allow us to interpret the crossover from a $Q^{-2}$ behavior to a $Q^{-1}$ behavior across the glass transition as a signature of a change from diffusive dynamics to discontinuous hopping of caged particles, as predicted in ref. 25.

2 Materials and methods

We used a widely studied colloidal clay,39–45 Laponite RD dispersions, prepared using the same protocol described in ref. 45. When dispersed in water Laponite develops a charged colloidal suspension of disks of 25 nm diameter and 0.9 nm thickness. All measurements have been performed using $D_2O$ (EURISO-TOP) of purity $\geq 99.9\%$ as a solvent. As recently shown the H/D isotopic substitution, required to gain contrast in neutron scattering measurements, does not qualitatively affect the aging behaviour of Laponite.46 The waiting time origin ($t_w = 0$) is the time at which the dispersion is filtered directly in glass tubes with a diameter of 10 mm for DLS and of 2 mm for XPCS and in quartz cells with dimensions of 30 mm $\times$ 40 mm $\times$ 4 mm for NSE measurements. To avoid CO$_2$ degradation all samples were prepared and sealed inside a glovebox under a nitrogen atmosphere. All experiments were performed at the same molar concentration of a $C_w = 3.0\%$ sample in salt free water. At this weight concentration the system forms a Wigner glass46,47 due to repulsive electrostatic interactions. This is a glass occurring in a dilute system which shares the main features of denser glasses, including a two-step decay.48–50

DLS measurements were performed with a multi-angle setup in the time range between $10^{-6}$ s and 1 s. A solid state laser with a wavelength of 642 nm and a power of 100 mW and single mode collecting fibers at five different scattering angles are used. Time autocorrelation functions are therefore simultaneously acquired at wavenumbers $Q = 6.2 \times 10^{-3}, 1.1 \times 10^{-3}, 1.5 \times 10^{-3}, 1.8 \times 10^{-3}$ and $2.1 \times 10^{-3}$ $\AA^{-1}$ by calculating the intensity autocorrelation function as $g_2(Q, t) = \frac{\langle I(Q, t_0)I(Q, t_0 + t)\rangle}{\langle I(Q, t_0)\rangle^2}$ where $\langle \ldots \rangle$ denotes the temporal average over $t_0$. DLS is used only when the system is ergodic in the early aging, also referred to as cage forming, regime characterized by a structural relaxation time with a waiting time exponential dependence $\tau_2(t_w) \approx e^{t_w/\tau}$.41

XPCS measurements were performed at the ID10 beamline at the European Synchrotron Radiation Facility (ESRF, Grenoble, France) in a $Q$-range between $3.1 \times 10^{-3}$ and $2.2 \times 10^{-2}$ $\AA^{-1}$ including the peak of the static structure factor occurring at $Q_{peak} \approx 1.6 \times 10^{-2}$ $\AA^{-1}$ as in the $H_2O$ solvent.47 Using an incident partially coherent X-ray beam with energy fixed at 8 keV a series of scattering images were recorded by using a charged coupled device (CCD) and the ensemble averaged intensity autocorrelation function $g_2(Q, t)$ was calculated by using a standard multi tau algorithm after having ensemble averaged over the detector pixels mapping onto a single $Q$ value.48 XPCS can thus be used when the system is non-ergodic in the full aging regime characterized by a waiting time power law dependence of the structural relaxation time $t_2(t_w) \approx t_w^\gamma$ with $\gamma \sim 1$.41

NSE measurements were performed at the spectrometer IN15 of the Institute Laue-Langevin (ILL, Grenoble, France) at larger wavevectors ($1.3 \times 10^{-2} < Q < 1.3 \times 10^{-1}$ $\AA^{-1}$) and at shorter relaxation times (up to $2 \times 10^{-7}$ s) with respect to DLS and XPCS. We used wavelengths of 10, 16 and 22.8 $\AA$ yielding time ranges (0.35–50) ns, (1.4–206) ns and (4.1–598) ns, respectively. While DLS and XPCS measure the normalized intensity correlation function $g_2(Q, t) = 1 + b[g_4(Q, t)]^2$ (Siegert relation), respectively through temporal averages (ergodic regime) and ensemble averages (non-ergodic regime), NSE directly accesses the intermediate scattering function $g_4(Q, t)$. We complemented the experimental measurements with MD simulations for a simple model of low-density glass-former, i.e. a 50–50 non-crystallising binary mixture of $N = 1000$ Yukawa particles of equal screening length $\xi$ and different repulsion strengths.49† The system was found50 to undergo a Wigner glass transition upon decreasing temperature $T$. To mimic the experimental situation, we performed a quench inside the glassy region at a fixed number density $\rho = 0.002984$. The system was equilibrated at high $T = 1.0 \times 10^{-3}$ and then instantaneously quenched to $T = 1.6 \times 10^{-5}$, below the glass transition occurring at $T_g \sim 1.7 \times 10^{-5}$. The waiting time origin was the time of the quench. Self intermediate scattering functions $F_i(Q, t)$ have been calculated for different wave vectors as a function of waiting time, averaging over 20 independent quenches to improve statistics.

3 Results

Fig. 1(a) shows the normalized intensity correlation functions measured by using DLS at initial waiting time ($t_w = 9$ min) for different $Q$-values (symbols) and the corresponding fits (full lines) obtained through a typical double exponential decay:

$$g_2(q, t) = b \left[ a e^{-\gamma t} + (1 - a) e^{-\xi t} \right]^2$$

where the parameters $a$ and $(1 - a)$ are the amplitudes of the two relaxation modes, $b$ is the coherence factor, $\gamma$ is the fast relaxation time connected to the microscopic motion of particles, $\tau_i$ is the slow relaxation time related to the structural rearrangement, and $\gamma$ (here $\gamma = 1$ (ref. 11 and 52)) and $\beta$ measure the distribution widths of the two relaxations.

The $Q$-dependence of the fast and slow relaxation times is reported in Fig. 1(b) at different waiting times. While $\tau_1$ shows a moderate waiting time dependence, $\tau_2$ increases significantly

† Lengths and times are measured in units of $\xi$ and $\xi/(m\bar{\epsilon})^{1/2}$ respectively, where $m$ is the mass of the particles and $\epsilon$ is the unit of energy. Temperature is measured in units of $\epsilon$ (i.e. $k_B = 1$ where $k_B$ is the Boltzmann constant).
with $t_w$. Both times are well described by power law fits $\sim Q^{-n}$ with $n \approx 2$ (solid lines in Fig. 1(b)). Hence both microscopic and structural relaxation times display an almost quadratic wave vector dependence in the DLS (early aging) regime, which is the signature of diffusive dynamics for both relaxations at these early waiting times. These findings are in agreement with previous studies on Laponite water suspensions.\textsuperscript{11,26,31,32}

Fig. 2(a) shows the dynamic structure factors measured by using NSE at different wavevectors (symbols) together with single stretched exponential fits (full lines). The corresponding fast relaxation times are shown in Fig. 2(b). We find that $\tau_1$ scales as $\sim Q^{-2}$ during the whole experiment. As reported in the inset of Fig. 2(b) the estimate of $\tau_1$ obtained from the NSE fits is in good agreement with that obtained by DLS, taking into account the large difference in $Q$ between these techniques. Since the studied sample experiences a sol to Wigner glass transition at $t_w \approx 600$ min (derived as in ref. 52), NSE results ensure that the microscopic relaxation time remarkably scales as $Q^{-2}$ both in the early aging and full aging regimes indicating that the short-time dynamics remains diffusive for all the investigated dynamical ranges even in the arrested state.

In Fig. 3(a) normalized intensity correlation functions probed by using XPCS in the full aging regime are shown at different $Q$-values (symbols). At these long waiting times the fast relaxation time $\tau_1$ is out of the XPCS detection window. Hence only the slow relaxation time $\tau_2$ can be measured and only the second term of eqn (1) is used to fit the data (full lines in Fig. 3(a)). We notice that in our case DLS measurements allow to probe relaxation times up to $\sim 10^{-1}$ s (higher limit in Fig. 1(b)), reached for the sample in the ergodic region at waiting time $t_w = 224$ min, while XPCS measurements permit to access relaxation times above $\sim 10^2$ s (lower limit in Fig. 3(b)) achieved for the sample in the non-ergodic region at waiting time $t_w = 743$ min. Fig. 3(b) shows the $Q$-dependence of $\tau_2$ at different waiting times (symbols) and the associated power law fits (full lines) as $\sim Q^{-n}$. In this regime we find $n = 1$ ruling out the diffusive dynamics. Therefore a crossover from the DLS early aging regime characterized by $\tau_2(Q) \propto Q^{-2}$ to the XPCS full aging regime characterized by $\tau_2(Q) \propto Q^{-1}$ is observed. As shown in Fig. 4 this crossover is also associated with a typical dual waiting time dependence of the structural relaxation time with $\tau_2(t_w) \propto e^{\alpha t_w}$ at short waiting times probed by DLS and $\tau_2(t_w) \propto t_w^\beta$ with $\beta > 1$ at long waiting times probed by XPCS. In both cases the intensity correlation functions are described by stretched exponentials at variance with the $\beta > 1$ behaviour found in previous studies\textsuperscript{29–32} and in rejuvenated samples,\textsuperscript{33} as fully discussed in ref. 53.

Fig. 1 (a) Normalized intensity correlation functions measured using DLS for different $Q$-values at $t_w = 9$ min. The solid lines are the fits obtained through eqn (1) with $\gamma = 1$. (b) $Q$-dependence of the fast $\tau_1$ and slow $\tau_2$ relaxation times at different waiting times. The solid lines are power law fits of the data as $\sim Q^{-n}$ where $n = 1.70 \pm 0.06$ for $\tau_1$ and $n = 2.02 \pm 0.19$ for $\tau_2$.

Fig. 2 (a) Dynamic structure factor obtained from NSE measurements for different $Q$-values at $t_w = 30$ min. The solid lines are stretched exponential fits with $\beta \sim 1$. (b) $Q$-dependence of the fast relaxation time at different waiting times. The solid lines are power law fits of the data as $\sim Q^{-n}$ where $n = 1.97 \pm 0.24$. Inset: comparison between fast relaxation times measured using DLS ($t_w = 9$ min) and NSE ($t_w = 84 960$ min) as a function of $Q/Q_{peak}$. The dashed line indicates the $Q^{-2}$ behaviour. The red vertical line indicates the position of the structure factor peak.
The combination of three complementary experimental techniques has allowed us to show that the fast relaxation mode remains diffusive both in ergodic and non-ergodic conditions at all waiting times. On the other hand, we observe that the structural relaxation time is characterized by two distinct \( Q \) behaviours in the two different regimes. This crossover could be then interpreted by a change from diffusive dynamics to discontinuous hopping of caged particles, as predicted in ref. 25 by lowering the temperature in a glass forming system. It remains to elucidate what happens in between the DLS and XPCS regimes, i.e. whether the change is discontinuous or not. Bhattacharyya et al.\(^\text{25}\) predicted a gradual change of the dynamics. To address this point we turn to MD simulations.

In Fig. 5(a) we report the MD self intermediate scattering functions (full lines) from MD simulations following a quench to \( T = 1.6 \times 10^{-5} \) at fixed waiting time \( t_w = 329 \) 328 MD units and different wavevectors, as reported in the labels. The dashed lines are the fitting curves obtained using the expression within the square brackets of eqn (1) with \( \gamma = 2 \). (b) \( Q \)-dependence of the slow relaxation time \( \tau_s \) extracted from the fits for selected values of \( t_w \). The dashed and full lines indicate respectively the \( Q^{-2} \) and \( Q^{-1} \) behaviours. The red vertical line indicates the position of the structure factor peak.

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In Fig. 5(a) we report the MD self intermediate scattering functions (full lines) at a fixed waiting time after a quench in the glassy state for several wavevectors. The microscopic dynamics is Newtonian, thereby the data are fitted by the double exponential decay within the square brackets of eqn (1) with \( \gamma = 2 \) and the corresponding \( \tau_s \) is not relevant to describe the experimental (Brownian) fast relaxation. We discuss only wavevectors small enough that the second exponential in eqn (1) is stretched (\( \beta < 1 \)), excluding large \( Q \) values where the dynamics becomes again ballistic due to the underlying microscopic dynamics.\(^\text{24}\) In the early aging regime, the correlators do not display the typical two-step decay, similar to what was observed in out-of-equilibrium simulations of other glass formers.\(^\text{25}\) We thus focus on the regime
occurring at larger waiting times, i.e. $t_w \geq 20,000$, where full aging starts and the double exponential describes the correlators, as shown by the fits in Fig. 5(a) (dashed lines). The corresponding $\tau_2$ is reported as a function of $Q$ in Fig. 5(b) for different values of the waiting time. We find that $\tau_2$ initially displays $Q^{-2}$ dependence at low and intermediate wave-vectors, in agreement with the DLS data of Fig. 1. Upon increasing $t_w$, while at low $Q$ (approaching the hydrodynamic regime) $\tau_2$ still tends to recover a diffusive behaviour ($Q^{-2}$), at intermediate $Q$ encompassing the main structure factor peak (see the vertical line in Fig. 5(b)) a clear power-law dependence $Q^{-n}$ with the exponent lowering and approaching unity at large $t_w$, is observed. At even larger $t_w$ the system becomes non-ergodic on the timescale of our simulations. Thus, in the full aging regime we observe a strongly non-diffusive dependence of $\tau_2$, approaching a $Q^{-1}$ behaviour, in full agreement with the XPCS data in the same $Q$-window. Interestingly, $n$ decreases continuously with increasing $t_w$ in agreement with theoretical predictions.25

4 Conclusions

In this study we have investigated the $Q$-dependence of both microscopic and structural relaxation times during the early aging and full aging regimes of a colloidal glass using multi-angle DLS, NSE and XPCS techniques, covering a wide range of wave-vectors and times. The experimental results have been complemented by MD simulations. We found that the microscopic relaxation time, $\tau_1$, characteristic of the short-time diffusion of a particle in the suspending medium, scales as $Q^{-2}$ during both early aging and full aging regimes, depicting a diffusive nature of particle motion. In contrast the slow relaxation time, $\tau_2$, associated with the structural rearrangement of the system, shows a transition from a $Q^{-2}$ diffusive behaviour in the liquid (or early aging) regime to a $Q^{-1}$ activated dynamics in the glass (or full aging) regime associated with a stretched behaviour of the correlation functions, in full agreement with recent theoretical predictions.25 Moreover this crossover is also associated with a dual waiting time dependence of $\tau_2$: $\tau_2(t_w) \propto e^{s_2}$ in the early aging regime and $\tau_2(t_w) \propto t_w^{s_2}$ in the full aging regime. Despite the peculiar and complex nature of Laponite,25 the reported experimental evidence is not specific to the studied system. Indeed, our results confirm and extend previous detections of non-diffusive/activated dynamics in the supercooled regime reported both for molecular liquids, such as water22 and ortho-terphenyl,21 and for colloidal hard spheres.24 Thus, our study of both relaxations in a colloidal glass-former should be considered as generic and be used as a reference for the description of the complex dynamics at fast and slow timescales of any glass-former.

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